UPS2 QS025 Model 9

1. Use the Newton-Raphson method to estimate  $\sqrt[3]{4}$  correct to three decimal places.

[7 marks]

- 2. A circle passes through the point (5,2) and touches the line y+x=9 at the point (3,6). Find the coordinates of the centre and the radius of the circle. Hence, state the standard equation of the circle. [7 marks]
- 3. Determine the general equation of the differential equation  $x \frac{dy}{dx} y = 3x^2$ .

Hence find the particular solution for y(2) = 0.

[7 marks]

- 4. Sketch, on the same coordinate axes, the curves  $y = e^x$  and  $y = 2 + 3e^{-x}$ . [2 marks] Calculate the area of the region bounded by the y-axis and the curves. [5 marks]
- 5. (a) Find the foci of  $4x^2 + 9y^2 = 36$  and sketch its graph. [4 marks]
  - (b) By using implicit differentiation, find the gradient of the tangent to the curve  $4x^2 + 9y^2 = 36$ . Hence, find the coordinates on the curve with gradient  $\frac{2}{9}$ .

[6 marks]

6. (a) Find 
$$\int \frac{3x}{e^x} dx$$
 [5 marks]

(b) Find the values of A, B and C which satisfy

$$\frac{x+2}{(1-x)(x^2+2)} = \frac{A}{1-x} + \frac{Bx+C}{x^2+2}$$
 [4 marks]

Hence, find 
$$\int \frac{x+2}{(1-x)(x^2+2)} dx$$
. [3 marks]

## **END OF QUESTION**

UPS2 QS025 Model 9

## **Final Answer**

1. 1.587

2. centre = 
$$(-2,1)$$
; radius =  $5\sqrt{2}$ ; the equation of circle is  $(x+2)^2 + (y-1)^2 = 50$ 

3. 
$$y = 3x^2 + cx$$
;  $y = 3x^2 - 6x$ 

- 4. Area=  $2.20 \text{ units}^2$
- 5. a) Foci =  $(\sqrt{5}, 0)$  and  $(-\sqrt{5}, 0)$ .

b) 
$$\frac{dy}{dx} = -\frac{4x}{9y}$$
; Coordinates  $= \left(\frac{3\sqrt{10}}{10}, -3\sqrt{\frac{2}{5}}\right)$  and  $\left(-\frac{3\sqrt{10}}{10}, 3\sqrt{\frac{2}{5}}\right)$ 

- 6. a)  $-3e^{-x}[x+1]+c$ 
  - b) A=1, B=1, C=0

$$-\ln|1-x| + \frac{1}{2}[\ln|x^2+2|] + C$$