

1. Find $\int \frac{1}{1+e^{-2x}} dx$. **[6 marks]**

2. Use the Trapezoidal Rule with $n = 4$ to approximate $\int_0^2 \frac{1}{1+x^2} dx$. Give your answer correct to four decimal places. **[7 marks]**

3. Sketch the graph of parabola with vertex at (3, -1) and focus (5, -1). Hence find the equation of the parabola. **[6 marks]**

4. Determine the general solution of $\frac{dy}{dx} = 9x^2 y \sqrt{x^3 - 1}$. Hence state y in terms of x when $y(1) = 1$. **[7 marks]**

5. A circle passes through the points (1, -1) and (3, 5). Given that the line $y = -\frac{2}{3}x + \frac{7}{3}$ passes through the center of the circle. Find the equation of the circle. **[12 marks]**

6. Find $\int 8x^2 e^{2x} dx$. Hence find the volume of the solid generated when the region bounded by the curve $y = 5xe^{-x}$ and the lines $x = 0, x = 1, y = 0$ is rotated through 2π about the x -axis. **[12 marks]**

END OF QUESTION

Final Answer

1. $\frac{1}{2} \ln|e^{2x} + 1| + C$

2. 1.1038

3. $(y + 1)^2 = 8(x - 3)$

4. $y = Ae^{2(x^3-1)^{\frac{3}{2}}}$; $y = e^{2(x^3-1)^{\frac{3}{2}}}$

5. $x^2 + y^2 + 2x - 6y - 10 = 0$

6. $2e^{2x}(2x^2 - 2x + 1) + C$; $\frac{25\pi}{4}(e^2 - 1) \text{ unit}^3$