

1. Show that  $\frac{1}{1-\sin\theta} + \frac{1}{1+\sin\theta} = 2\sec^2\theta$ .
2. Show that  $\cot A + \tan 2A = \cot A \sec 2A$ .
3. Solve the equation  $3\cos 2\theta + \cos\theta = 2$  for  $0^\circ < \theta < 360^\circ$ .
4. If  $t = \tan \frac{\theta}{2}$ , show that  $\tan \theta = \frac{2t}{1-t^2}$ . Hence, solve the equation  $3\cos\theta + 2\sin\theta - 3 = 0$  for  $0 \leq \theta \leq 2\pi$ .
5. Express  $4\cos x - 3\sin x$  in the form  $R\cos(x+\theta)$ , where  $R > 0$  and  $\theta$  is acute angle.  
Hence
  - a) State the maximum and minimum value for  $8 - 4\cos x + 3\sin x$ .
  - b) Solve the equation  $4\cos x - 3\sin x = -\frac{5}{2}$  for  $0^\circ \leq x \leq 360^\circ$ .

**Answer :**

- 3)  $\theta = 33.6^\circ, 180^\circ, 326.4^\circ$
- 4)  $\theta = 0, 1.18, 2\pi$
- 5)  $5\cos(x+36.9^\circ)$ 
  - a) maximum value = 13, minimum value = 3
  - b)  $83.1^\circ, 203.1^\circ$